Yet another F-space sample

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In this talk we will explore a new growth condition on Young functions, which we call Mulholland condition, pertaining to the mathematician H. P. Mulholland, who studied these functions for the first time, albeit in a different context. We construct a non-trivial Young function Ω which satisfies Mulholland condition and Δ_2 -condition. We then associate exotic *F*-norms to the vector space $X_1 \oplus X_2$, where X_1 and X_2 are Banach spaces, using the function Ω . This *F*-space contains the Banach space X_1 and X_2 as maximal Banach subspace. Further, the Banach envelope $(X_1 \oplus X_2, \|.\|_{\Omega_o})$ of this *F*-space corresponds to the Young function Ω_o whose characteristic function is an asymptotic line to the characteristic function of the Young function Ω . Thus this *F*-space serves as the interpolation space for Banach spaces X_1 and $(X_1 \oplus X_2, \|.\|_{\Omega_o})$.